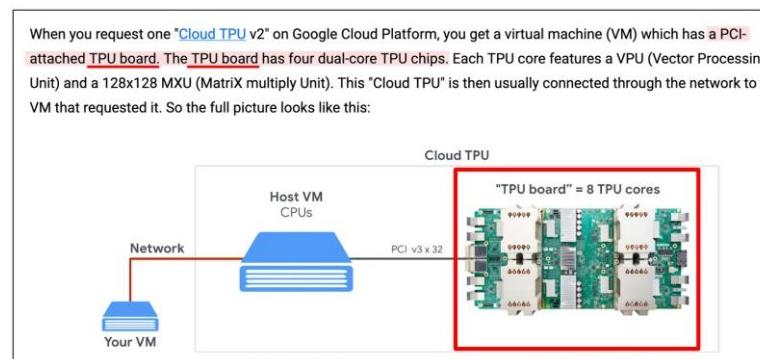
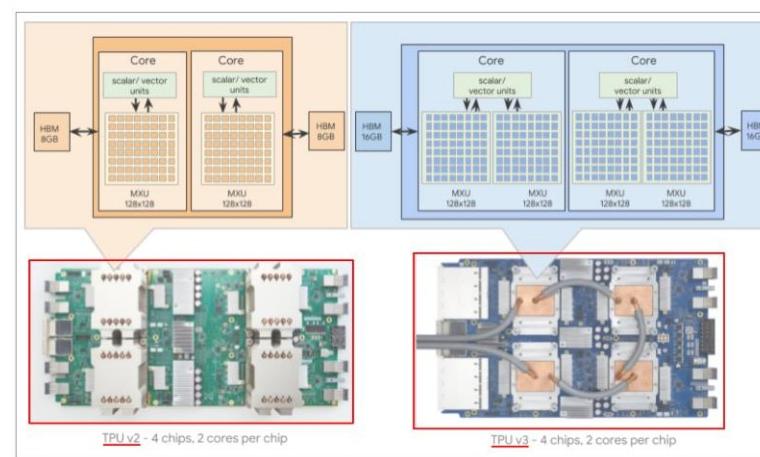


EXHIBIT A

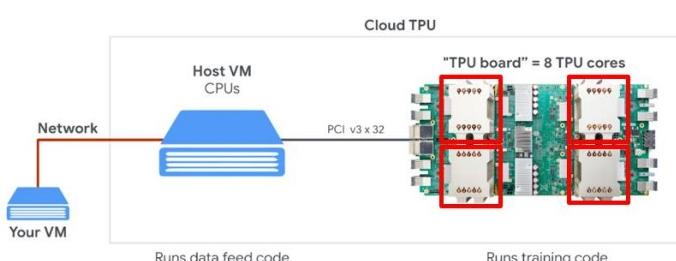
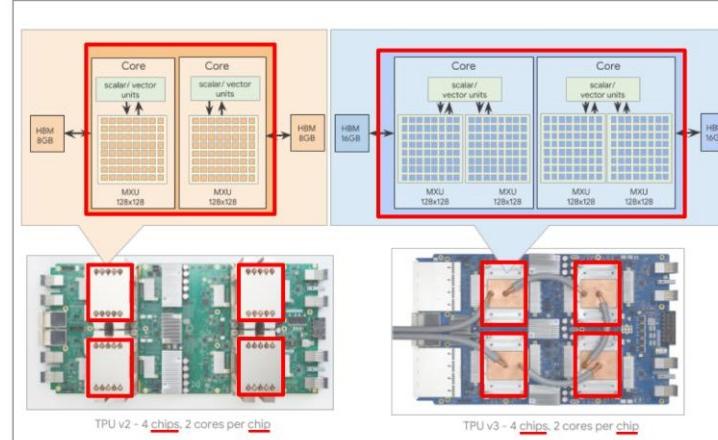
Exhibit A

U.S. Pat. No. 9,218,156

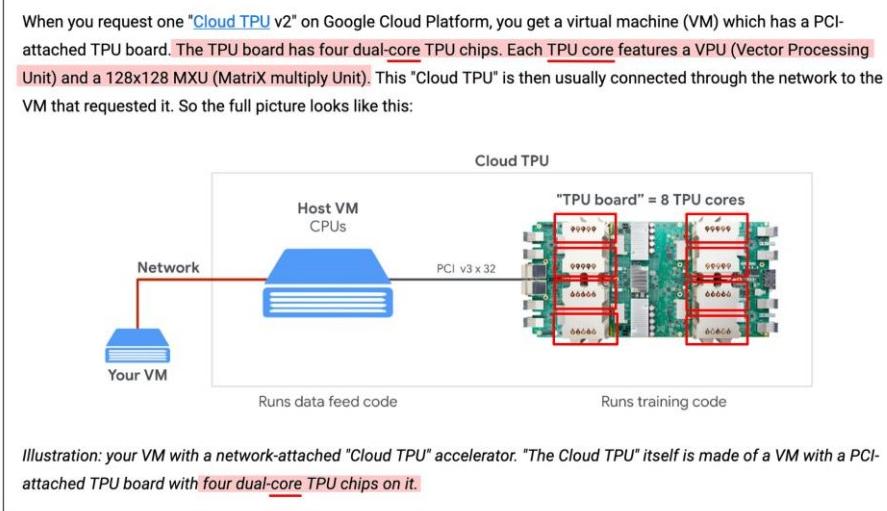
Claim 7

'156 PATENT	INFRINGEMENT EVIDENCE
<p>7. A device comprising:</p> <p>at least one first low precision high-dynamic range (LPHDR) execution unit adapted to execute a first operation on a first input signal representing a first numerical value to produce a first output signal representing a second numerical value,</p> <p>wherein the dynamic range of the possible valid inputs to the first operation is at least as wide as from 1/1,000,000 through 1,000,000 and for at least X=5% of the possible valid inputs to the first operation, the statistical mean, over repeated execution of the first operation on each specific input from the at least X% of the possible valid inputs to the first operation, of the numerical values represented by the first output signal of the LPHDR unit executing the first operation on that input differs by at least Y=0.05% from the result of an exact mathematical calculation of the first operation on the numerical values of that same input;</p> <p>at least one first computing device adapted to control the operation of the at least one first LPHDR execution unit</p> <p>wherein the at least one first computing device comprises at least one of a central processing unit (CPU), a graphics processing unit (GPU), a field programmable gate array (FPGA), a microcode-based processor, a hardware sequencer, and a state machine; and,</p> <p>wherein the number of LPHDR execution units in the device exceeds by at least one hundred the non-negative integer number of execution units in the device adapted to execute at least the operation of multiplication on floating point numbers that are at least 32 bits wide.</p>	<p>As demonstrated below, the Accused Products include multiple components that, separately and independently, meet all the requirements of the claimed “device.” For example, a “TPU Board” satisfies these requirements:</p> <div style="border: 1px solid black; padding: 10px; margin-bottom: 10px;"> <p>When you request one “Cloud TPU v2” on Google Cloud Platform, you get a virtual machine (VM) which has a PCI-attached TPU board. The TPU board has four dual-core TPU chips. Each TPU core features a VPU (Vector Processing Unit) and a 128x128 MXU (Matrix multiply Unit). This “Cloud TPU” is then usually connected through the network to the VM that requested it. So the full picture looks like this:</p>  <p>Illustration: your VM with a network-attached “Cloud TPU” accelerator. “The Cloud TPU” itself is made of a VM with a PCI-attached TPU board with four dual-core TPU chips on it.</p> </div> <p>https://codelabs.developers.google.com/codelabs/keras-flowers-convnets/#2¹</p> <div style="text-align: center;">  <p>TPU v2 - 4 chips, 2 cores per chip</p> <p>TPU v3 - 4 chips, 2 cores per chip</p> </div> <p>https://cloud.google.com/tpu/docs/system-architecture</p>

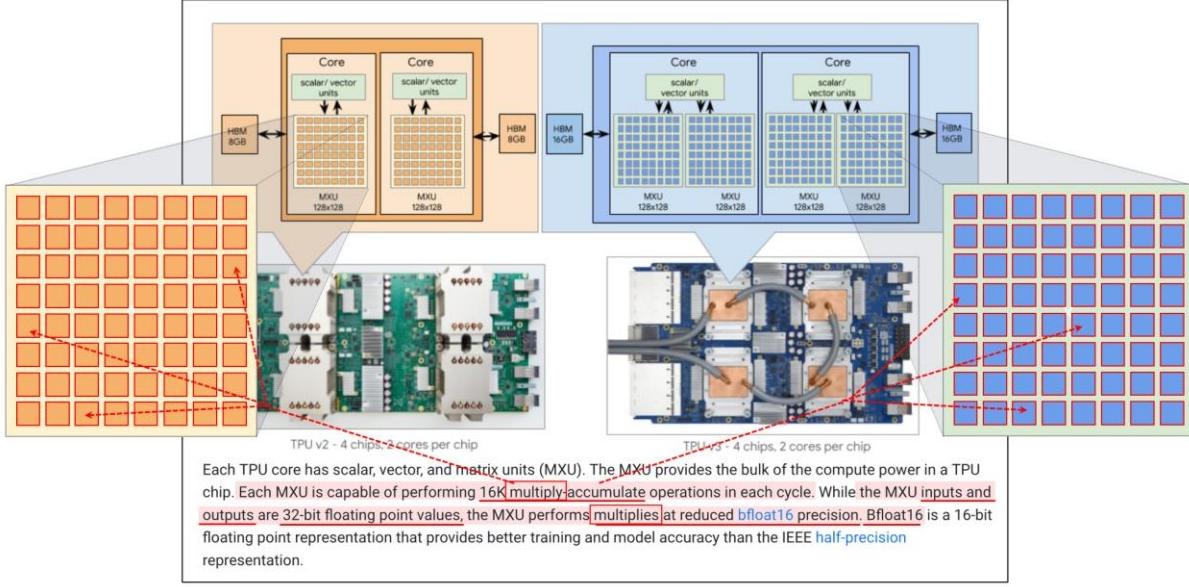
¹ Unless indicated otherwise, color-coded annotations have been added in order to identify relevant components and features of the Accused Products.

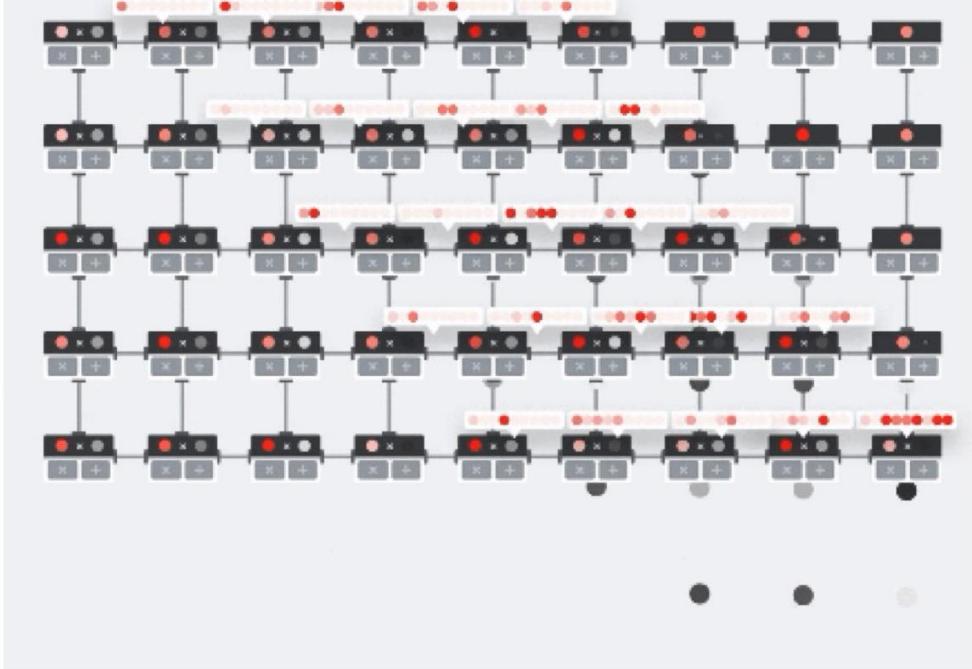
'156 PATENT	INFRINGEMENT EVIDENCE
<p>7. A <u>device</u> comprising:</p> <p>at least one first low precision high-dynamic range (LPHDR) execution unit adapted to execute a first operation on a first input signal representing a first numerical value to produce a first output signal representing a second numerical value,</p> <p>wherein the dynamic range of the possible valid inputs to the first operation is at least as wide as from 1/1,000,000 through 1,000,000 and for at least X=5% of the possible valid inputs to the first operation, the statistical mean, over repeated execution of the first operation on each specific input from the at least X% of the possible valid inputs to the first operation, of the numerical values represented by the first output signal of the LPHDR unit executing the first operation on that input differs by at least Y=0.05% from the result of an exact mathematical calculation of the first operation on the numerical values of that same input;</p> <p>at least one first computing device adapted to control the operation of the at least one first LPHDR execution unit</p> <p>wherein the at least one first computing device comprises at least one of a central processing unit (CPU), a graphics processing unit (GPU), a field programmable gate array (FPGA), a microcode-based processor, a hardware sequencer, and a state machine; and,</p> <p>wherein the number of LPHDR execution units in the device exceeds by at least one hundred the non-negative integer number of execution units in the device adapted to execute at least the operation of multiplication on floating point numbers that are at least 32 bits wide.</p>	<p>As demonstrated below, the Accused Products include multiple components that, separately and independently, meet all the requirements of the claimed “device.” For example, a “TPU Chip” satisfies these requirements:</p> <div style="border: 1px solid black; padding: 10px;"> <p>When you request one “Cloud TPU v2” on Google Cloud Platform, you get a virtual machine (VM) which has a PCI-attached TPU board. The TPU board has four dual-core <u>TPU chips</u>. Each TPU core features a VPU (Vector Processing Unit) and a 128x128 MXU (Matrix multiply Unit). This “Cloud TPU” is then usually connected through the network to the VM that requested it. So the full picture looks like this:</p>  <p>Illustration: your VM with a network-attached “Cloud TPU” accelerator. The Cloud TPU itself is made of a VM with a PCI-attached TPU board with four dual-core <u>TPU chips</u> on it.</p> <p>https://codelabs.developers.google.com/codelabs/keras-flowers-convnets/#2</p>  <p>https://cloud.google.com/tpu/docs/system-architecture</p> <p>See also generally Norrie et al., “Google’s Training Chips Revealed: TPUv2 and TPUv3” (Presented at HotChips Conference, Aug. 2020)</p> </div>

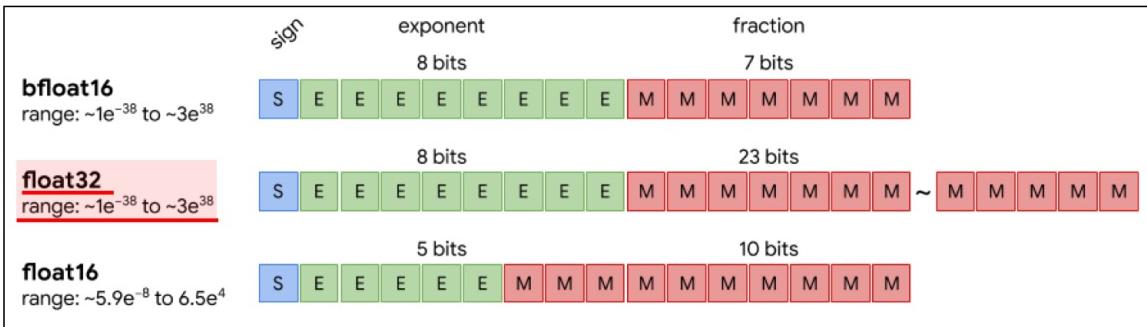
² Unless indicated otherwise, color-coded annotations have been added to the figures in this chart to highlight relevant teachings of the prior art.

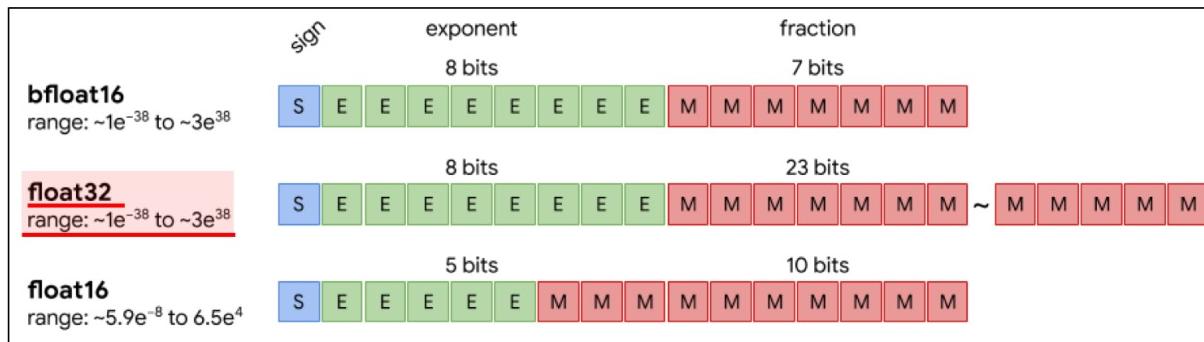
'156 PATENT	INFRINGEMENT EVIDENCE
<p>7. A <u>device</u> comprising:</p> <p>at least one first low precision high-dynamic range (LPHDR) execution unit adapted to execute a first operation on a first input signal representing a first numerical value to produce a first output signal representing a second numerical value,</p> <p>wherein the dynamic range of the possible valid inputs to the first operation is at least as wide as from 1/1,000,000 through 1,000,000 and for at least X=5% of the possible valid inputs to the first operation, the statistical mean, over repeated execution of the first operation on each specific input from the at least X% of the possible valid inputs to the first operation, of the numerical values represented by the first output signal of the LPHDR unit executing the first operation on that input differs by at least Y=0.05% from the result of an exact mathematical calculation of the first operation on the numerical values of that same input;</p> <p>at least one first computing device adapted to control the operation of the at least one first LPHDR execution unit</p> <p>wherein the at least one first computing device comprises at least one of a central processing unit (CPU), a graphics processing unit (GPU), a field programmable gate array (FPGA), a microcode-based processor, a hardware sequencer, and a state machine; and,</p> <p>wherein the number of LPHDR execution units in the device exceeds by at least one hundred the non-negative integer number of execution units in the device adapted to execute at least the operation of multiplication on floating point numbers that are at least 32 bits wide.</p>	<p>As demonstrated below, the Accused Products include multiple components that, separately and independently, meet all the requirements of the claimed “device.” For example, a “TPU Core” satisfies these requirements:</p> <p>When you request one “Cloud TPU v2” on Google Cloud Platform, you get a virtual machine (VM) which has a PCI-attached TPU board. The TPU board has four dual-core TPU chips. Each TPU core features a VPU (Vector Processing Unit) and a 128x128 MXU (Matrix multiply Unit). This “Cloud TPU” is then usually connected through the network to the VM that requested it. So the full picture looks like this:</p>  <p>Illustration: your VM with a network-attached “Cloud TPU” accelerator. The Cloud TPU itself is made of a VM with a PCI-attached TPU board with four dual-core TPU chips on it.</p> <p>https://codelabs.developers.google.com/codelabs/keras-flowers-convnets/#2</p>  <p>https://cloud.google.com/tpu/docs/system-architecture</p>

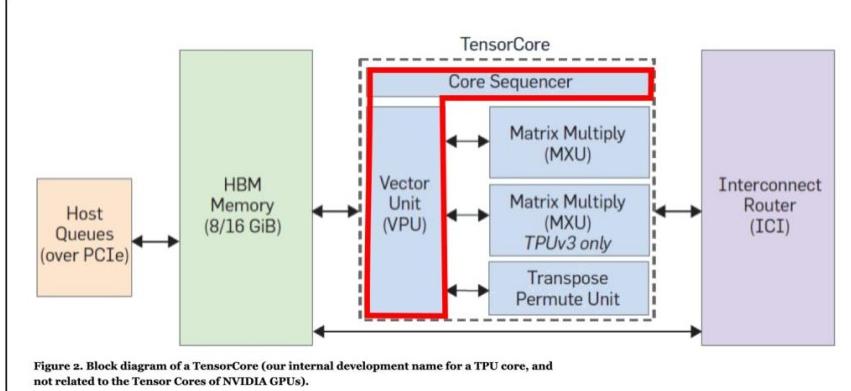
'156 PATENT	INFRINGEMENT EVIDENCE
<p>7. A <u>device</u> comprising:</p> <p>at least one first low precision high-dynamic range (LPHDR) execution unit adapted to execute a first operation on a first input signal representing a first numerical value to produce a first output signal representing a second numerical value,</p> <p>wherein the dynamic range of the possible valid inputs to the first operation is at least as wide as from 1/1,000,000 through 1,000,000 and for at least X=5% of the possible valid inputs to the first operation, the statistical mean, over repeated execution of the first operation on each specific input from the at least X% of the possible valid inputs to the first operation, of the numerical values represented by the first output signal of the LPHDR unit executing the first operation on that input differs by at least Y=0.05% from the result of an exact mathematical calculation of the first operation on the numerical values of that same input;</p> <p>at least one first computing device adapted to control the operation of the at least one first LPHDR execution unit</p> <p>wherein the at least one first computing device comprises at least one of a central processing unit (CPU), a graphics processing unit (GPU), a field programmable gate array (FPGA), a microcode-based processor, a hardware sequencer, and a state machine; and,</p> <p>wherein the number of LPHDR execution units in the device exceeds by at least one hundred the non-negative integer number of execution units in the device adapted to execute at least the operation of multiplication on floating point numbers that are at least 32 bits wide.</p>	<p style="text-align: center;">Figure 3. TPUv2 chip floor plan.</p> <p style="text-align: center;">Figure 3. TPUv2 chip floor plan.</p> <p style="text-align: center;">https://cacm.acm.org/magazines/2020/7/245702-a-domain-specific-supercomputer-for-training-deep-neural-networks</p> <p style="text-align: center;">Figure 2. Block diagram of a TensorCore (our internal development name for a TPU core, and not related to the Tensor Cores of NVIDIA GPUs).</p> <p style="text-align: center;">Figure 2. Block diagram of a TensorCore (our internal development name for a TPU core, and not related to the Tensor Cores of NVIDIA GPUs).</p> <p style="text-align: center;"><i>Id.</i></p>

'156 PATENT	INFRINGEMENT EVIDENCE																
<p>7. A device comprising:</p> <p>at least one first low precision high-dynamic range (LPHDR) execution unit adapted to execute a first operation on a first input signal representing a first numerical value to produce a first output signal representing a second numerical value,</p> <p>wherein the dynamic range of the possible valid inputs to the first operation is at least as wide as from 1/1,000,000 through 1,000,000 and for at least X=5% of the possible valid inputs to the first operation, the statistical mean, over repeated execution of the first operation on each specific input from the at least X% of the possible valid inputs to the first operation, of the numerical values represented by the first output signal of the LPHDR unit executing the first operation on that input differs by at least Y=0.05% from the result of an exact mathematical calculation of the first operation on the numerical values of that same input;</p> <p>at least one first computing device adapted to control the operation of the at least one first LPHDR execution unit</p> <p>wherein the at least one first computing device comprises at least one of a central processing unit (CPU), a graphics processing unit (GPU), a field programmable gate array (FPGA), a microcode-based processor, a hardware sequencer, and a state machine; and,</p> <p>wherein the number of LPHDR execution units in the device exceeds by at least one hundred the non-negative integer number of execution units in the device adapted to execute at least the operation of multiplication on floating point numbers that are at least 32 bits wide.</p>	 <p>The diagram illustrates the TPU v2 and v3 system architecture. It shows two main components: TPU v2 and TPU v3. TPU v2 consists of four chips, each containing two cores (scalar/vector units) and four MXU units (128x128). TPU v3 consists of four chips, each containing two cores (scalar/vector units) and six MXU units (128x128). Both architectures include HBM memory (8GB or 16GB) connected to the cores and MXU units. The MXU units are highlighted in orange and blue, representing different configurations. The diagram also shows a close-up of the internal structure of a core and MXU unit, illustrating the 128x128 matrix units.</p> <p>https://cloud.google.com/tpu/docs/system-architecture</p> <table border="1" data-bbox="777 845 1924 1171"> <thead> <tr> <th></th> <th>sign</th> <th>exponent</th> <th>fraction</th> </tr> </thead> <tbody> <tr> <td>bfloat16 range: $\sim 1e^{-38}$ to $\sim 3e^{38}$</td> <td>S</td> <td>E E E E E E E</td> <td>M M M M M M M</td> </tr> <tr> <td>float32 range: $\sim 1e^{-38}$ to $\sim 3e^{38}$</td> <td>S</td> <td>E E E E E E E</td> <td>M M M M M M M ~ M M M M M</td> </tr> <tr> <td>float16 range: $\sim 5.9e^{-8}$ to $6.5e^4$</td> <td>S</td> <td>E E E E E</td> <td>M M M M M M M M M M</td> </tr> </tbody> </table> <p>https://cloud.google.com/tpu/docs/bfloat16</p>		sign	exponent	fraction	bfloat16 range: $\sim 1e^{-38}$ to $\sim 3e^{38}$	S	E E E E E E E	M M M M M M M	float32 range: $\sim 1e^{-38}$ to $\sim 3e^{38}$	S	E E E E E E E	M M M M M M M ~ M M M M M	float16 range: $\sim 5.9e^{-8}$ to $6.5e^4$	S	E E E E E	M M M M M M M M M M
	sign	exponent	fraction														
bfloat16 range: $\sim 1e^{-38}$ to $\sim 3e^{38}$	S	E E E E E E E	M M M M M M M														
float32 range: $\sim 1e^{-38}$ to $\sim 3e^{38}$	S	E E E E E E E	M M M M M M M ~ M M M M M														
float16 range: $\sim 5.9e^{-8}$ to $6.5e^4$	S	E E E E E	M M M M M M M M M M														

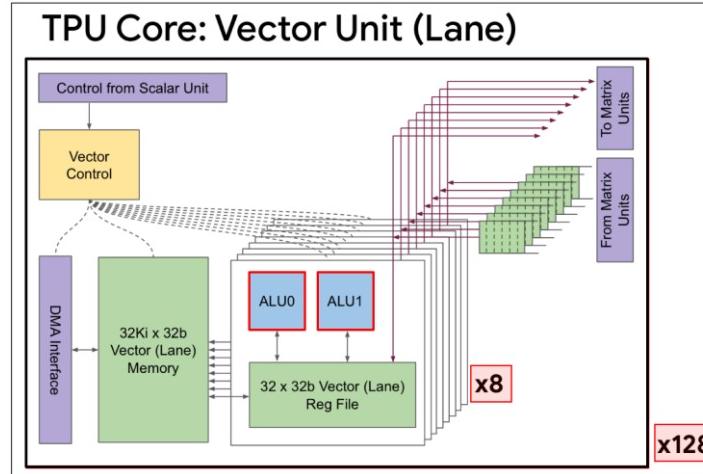
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<p>7. A device comprising:</p> <p>at least one first low precision high-dynamic range (LPHDR) execution unit adapted to execute a first operation on a first input signal representing a first numerical value to produce a first output signal representing a second numerical value,</p> <p>wherein the dynamic range of the possible valid inputs to the first operation is at least as wide as from 1/1,000,000 through 1,000,000 and for at least X=5% of the possible valid inputs to the first operation, the statistical mean, over repeated execution of the first operation on each specific input from the at least X% of the possible valid inputs to the first operation, of the numerical values represented by the first output signal of the LPHDR unit executing the first operation on that input differs by at least Y=0.05% from the result of an exact mathematical calculation of the first operation on the numerical values of that same input;</p> <p>at least one first computing device adapted to control the operation of the at least one first LPHDR execution unit</p> <p>wherein the at least one first computing device comprises at least one of a central processing unit (CPU), a graphics processing unit (GPU), a field programmable gate array (FPGA), a microcode-based processor, a hardware sequencer, and a state machine; and,</p> <p>wherein the number of LPHDR execution units in the device exceeds by at least one hundred the non-negative integer number of execution units in the device adapted to execute at least the operation of multiplication on floating point numbers that are at least 32 bits wide.</p>	<ul style="list-style-type: none"> “Each of the cores on a TPU device can execute user computations (XLA ops) independently.” https://cloud.google.com/tpu/docs/system-architecture#pod “TPUs use a VLIW architecture to express instruction-level parallelism to the many compute units of a TensorCore. XLA uses standard VLIW compilation techniques including loop unrolling, instruction scheduling, and software pipelining to keep all compute units busy and to simultaneously move data through the memory hierarchy to feed them.” https://cacm.acm.org/magazines/2020/7/245702-a-domain-specific-supercomputer-for-training-deep-neural-networks/fulltext “The Core Sequencer fetches VLIW (<i>Very Long Instruction Word</i>) instructions from the core's on-chip, software-managed Instruction Memory (Imem), executes scalar operations using a 4K 32-bit scalar data memory (Smem) and 32 32-bit scalar registers (Sregs), and forwards vector instructions to the VPU. The 322-bit VLIW instruction can launch eight operations: two scalar, two vector ALU, vector load and store, and a pair of slots that queue data to and from the matrix multiply and transpose units. The XLA compiler schedules loading Imem via independent overlays of code, as unlike conventional CPUs, there is no instruction cache.” <i>Id.</i> “The Vector Processing Unit (VPU) performs vector operations using a large on-chip <i>vector memory</i> (Vmem) with 32K 128 x 32-bit elements (16MiB), and 32 2D <i>vector registers</i> (Vregs) that each contain 128 x 8 32-bit elements (4 KiB). The VPU streams data to and from the MXU through decoupling FIFOs. The VPU collects and distributes data to Vmem via <i>data-level parallelism</i> (2D matrix and vector functional units) and <i>instruction-level parallelism</i> (8 operations per instruction).” <i>Id.</i>  <p>Figure 2. Block diagram of a TensorCore (our internal development name for a TPU core, and not related to the Tensor Cores of NVIDIA GPUs).</p>

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